

## Unit-II

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xxx ① Discuss conditions for interference of light and explain biprism (fresnel) experiment for finding wavelength.

\*\* ② Explain Fringes observed when wedge shaped film illuminated by monochromatic light.

\*\* ③ Describe arrangement to observe Newton's rings by reflected light and find wavelength.

\*\* ④ Explain interference fringes in Lloyd's mirror arrangement.

\*\* ⑤ Construction & working of Michelson Interferometer.

⑥ Determination of thickness of transparent material used in a prism.

⑦ Determination of difference in wavelengths of sodium  $D_1, D_2$  line / spectral line.

xxx Explain cosine law

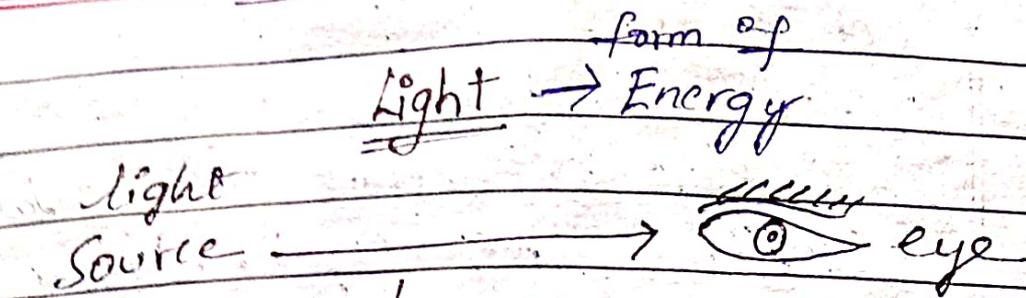
① formation of colours of thin film

② Spatial coherence

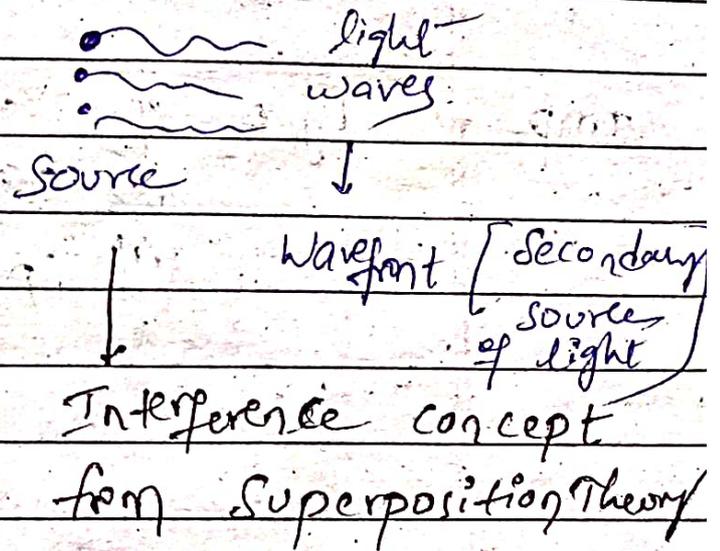
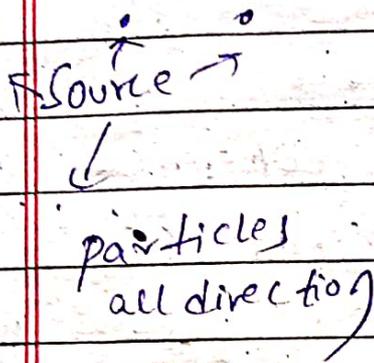
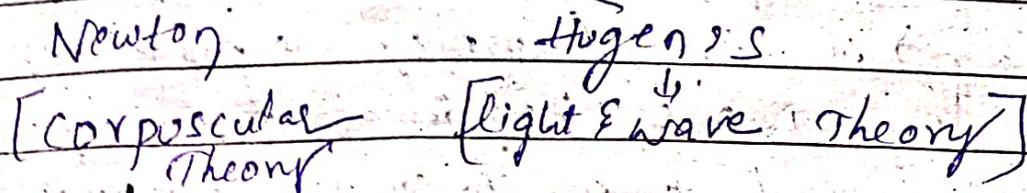
③ Difference b/w biprism & Lloyd's mirror

④ Types of fringes

# Introduction

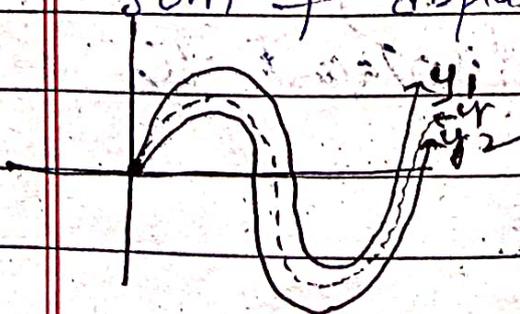


Study  $\rightarrow$  Optics



## Principle of Superposition

When two or more waves travelling through a medium superimpose each other then a new wave is formed whose resultant displacement is algebraic sum of displacements of individual waves



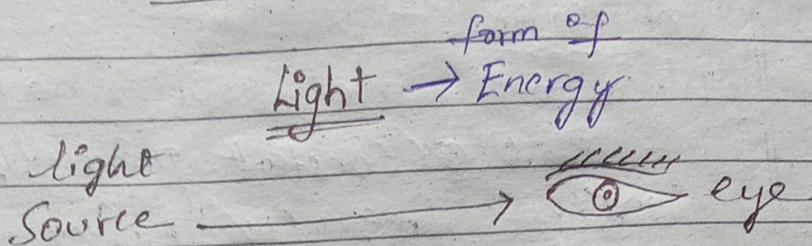
$$y = y_1 \pm y_2$$

$$y = y_1 + y_2 \quad \phi = 2n\pi$$

$$y = y_1 - y_2 \quad \phi = (2n+1)\pi$$

$\phi$  = phase difference

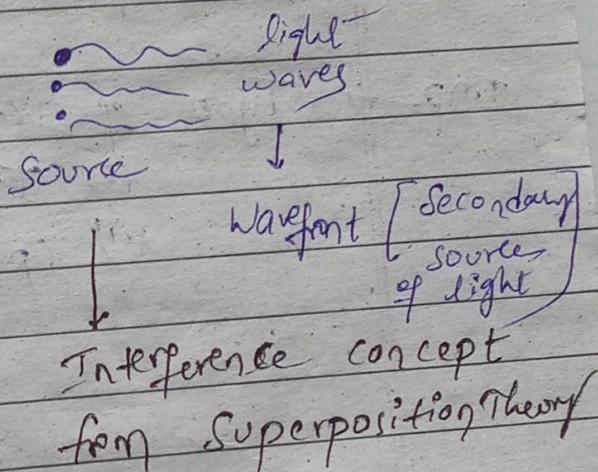
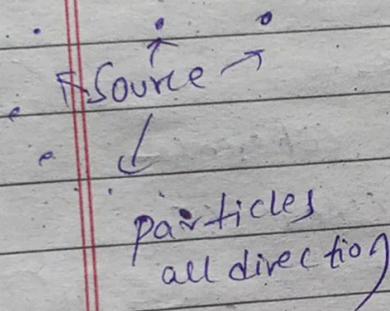
# Introduction



Study  $\rightarrow$  Optics

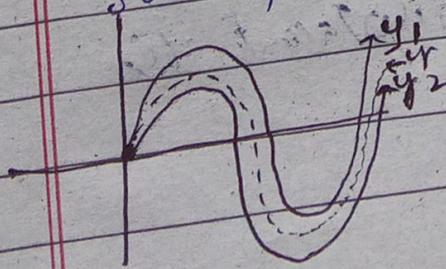
Newton  
[Corpuscular Theory]

Hugen's  
[light & wave Theory]



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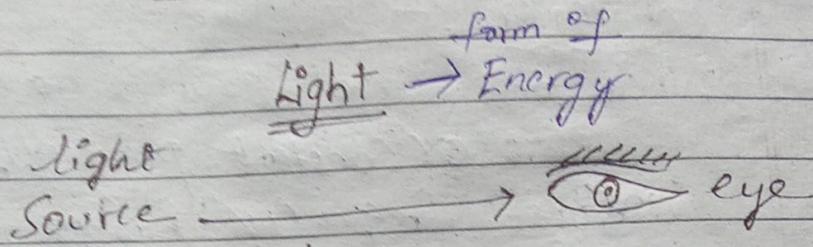
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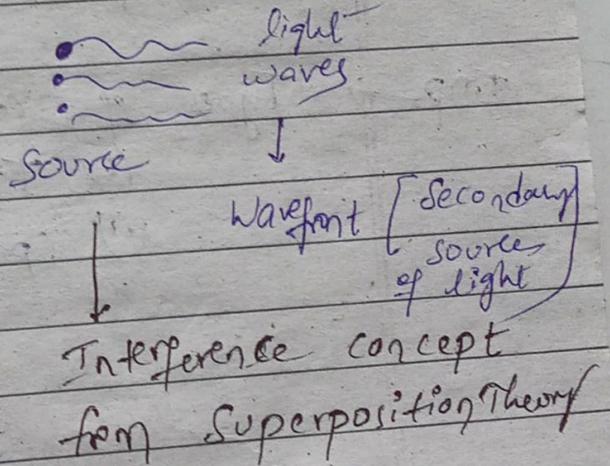
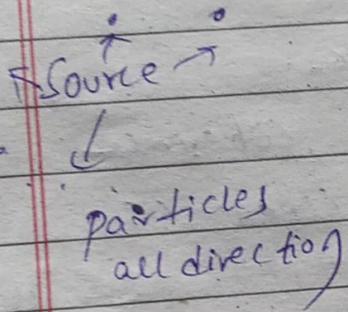
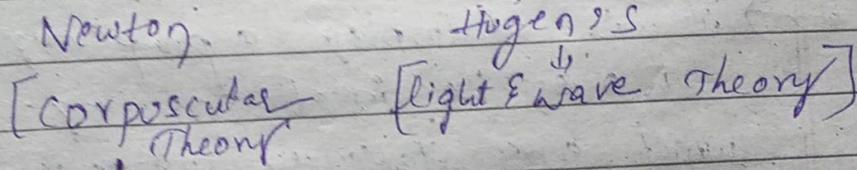
$$y = y_1 + y_2 \quad \phi = 2n\pi$$

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# Introduction

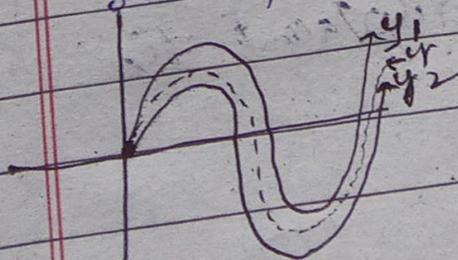


Study  $\rightarrow$  Optics



## Principle of Superposition

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$$y = y_1 + y_2$$

$\phi =$  phase difference

$$y = y_1 + y_2 \quad y = y_1 + y_2 \quad \phi = 2n\pi$$

$$y = y_1 - y_2 \quad \phi = (2n+1)\pi$$

coherence =  $\text{coherence} \rightarrow \text{coherence}$

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Coherence :-

→ When two wave sources have zero or constant phase difference and same frequency & same wave form they are called coherent sources.

This phenomenon is called coherence → it is simply a property of waves i.e. ideal property which gives stationary interference.

Imp → Types of coherence

- (i) Temporal coherence
- (ii) spatial coherence

phase difference - difference b/w position of 2 waves when they are in same direction used to compare displacement etc.

Interference is the phenomenon where the superposition of 2/more waves results in modification of resultant light intensity distribution

② what is Interference & conditions for interference of lights and types of Interference.

Interference:-

The phenomenon of modification of redistribution of intensity of light in the region of superposition is called interference.

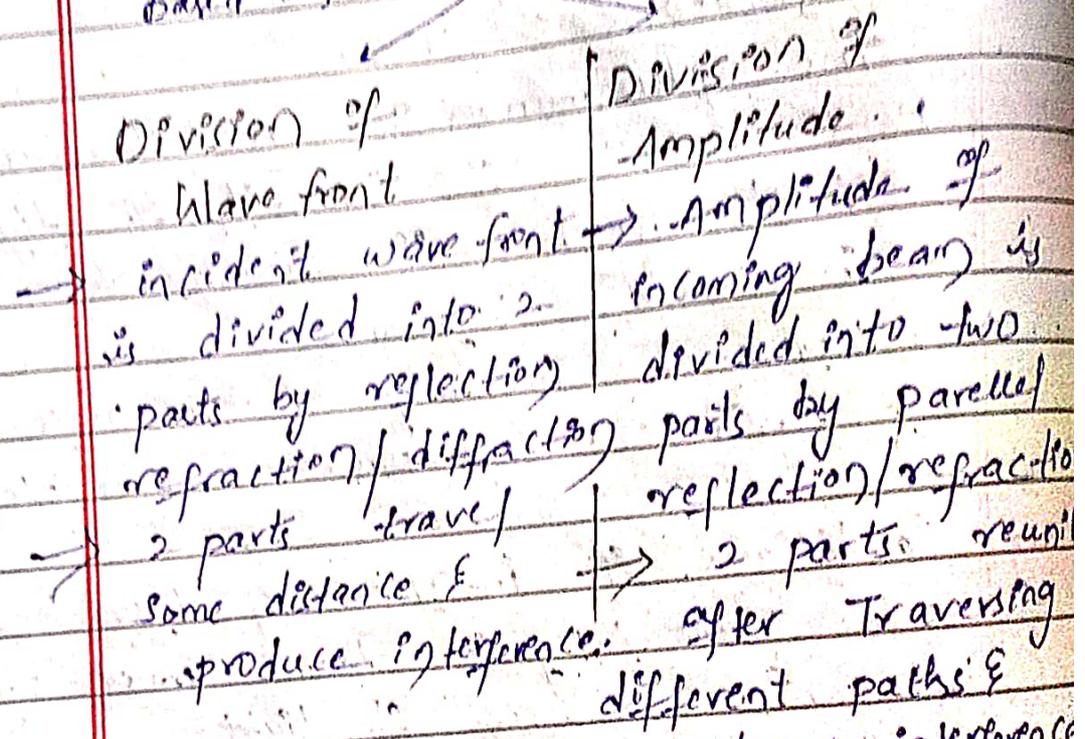
→ interference basically takes place based on superposition principle.

Conditions of interference of light:-

- (i) The two interfering beams must originate from same source of light and the sources must be coherent sources i.e. the <sup>initial</sup> ~~phase~~ <sup>phase</sup> difference must be zero or constant.
- (ii) Two interfering waves must propagate almost in the same direction or the wavefronts intersect at a very small angle.
- (iii) The original source of light must emit light of single wavelength i.e. Monochromatic source of light.
- (iv) The waves must have same period and wavelength also amplitudes must be equal (or) very nearly equal.

# Types of interference

interference is of 2 types  
based on how it is formed.



Eg:- Fresnel's biprism, Lloyd's mirror.

Eg:- Newton's ring, Michelson's Interferometer.

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## Types of interference

interference is of 2 types based on how it formed.

Division of wave front

→ incident wave front is divided into 2 parts by reflection/refraction/diffraction  
→ 2 parts travel some distance & produce interference.

Division of Amplitude

→ Amplitude of incoming beam is divided into two parts by parallel reflection/refraction.  
→ 2 parts reunite after traversing different paths & produces interference.

Eg: Fresnel's biprism, Lloyd's mirror.

Eg: Newton rings, Michelson's Interferometer

① Explain and find

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NOTE:  
(i) S  
(ii)

- ① Explain Fresnel's Bi-prism experiment and derive an expression for finding wavelength.

Bi-prism:-

Bi-prism is a combination of two acute prisms placed base to base.

This combination is obtained from an optically plane glass plate by proper grinding and polishing. The obtuse angle of prism is about  $179^\circ$  and other angles are about  $0.5^\circ$  ( $30'$ ) each.

Bi-prism Action:-

The bi-prism produce two coherent images of given slit which are separated by a certain distance and act as two coherent sources.

Experimental Setup:-

A optical bench carrying 4 stands, the first one for adjustable slit, second one for bi-prism, third one for convex lens and lastly 4th one for eyepiece i.e screen.

NOTE:-

(i) Stands can be moved along bench

(ii) Slit & bi-prism can be rotated in their own planes.

## procedure :- or Formation of interference :-

A narrow slit  $S$  is illuminated with a monochromatic source of light of wavelength " $\lambda$ " and is allowed to fall symmetrically on a biprism. The intersection of two inclined faces forming obtuse angle must be adjusted accurately parallel to slit.

→ The edge  $B$  divides incident wave front into 2 parts.

→ 1st part passes through upper half  $ABE$  of prism is deviated through small angle towards lower half of diagram & appears to diverge from  $S_1$ .

→ 2nd part passes through lower half  $CBE$  deviated through lower half towards upper half & appears to diverge from  $S_2$ .

→ Hence  $S_1$  and  $S_2$  serve as coherent sources resulting in 2 wave fronts intersect and give interference pattern which is observed by eye piece.

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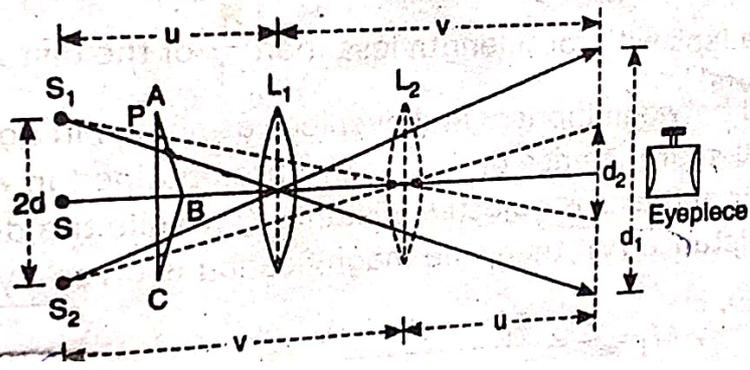
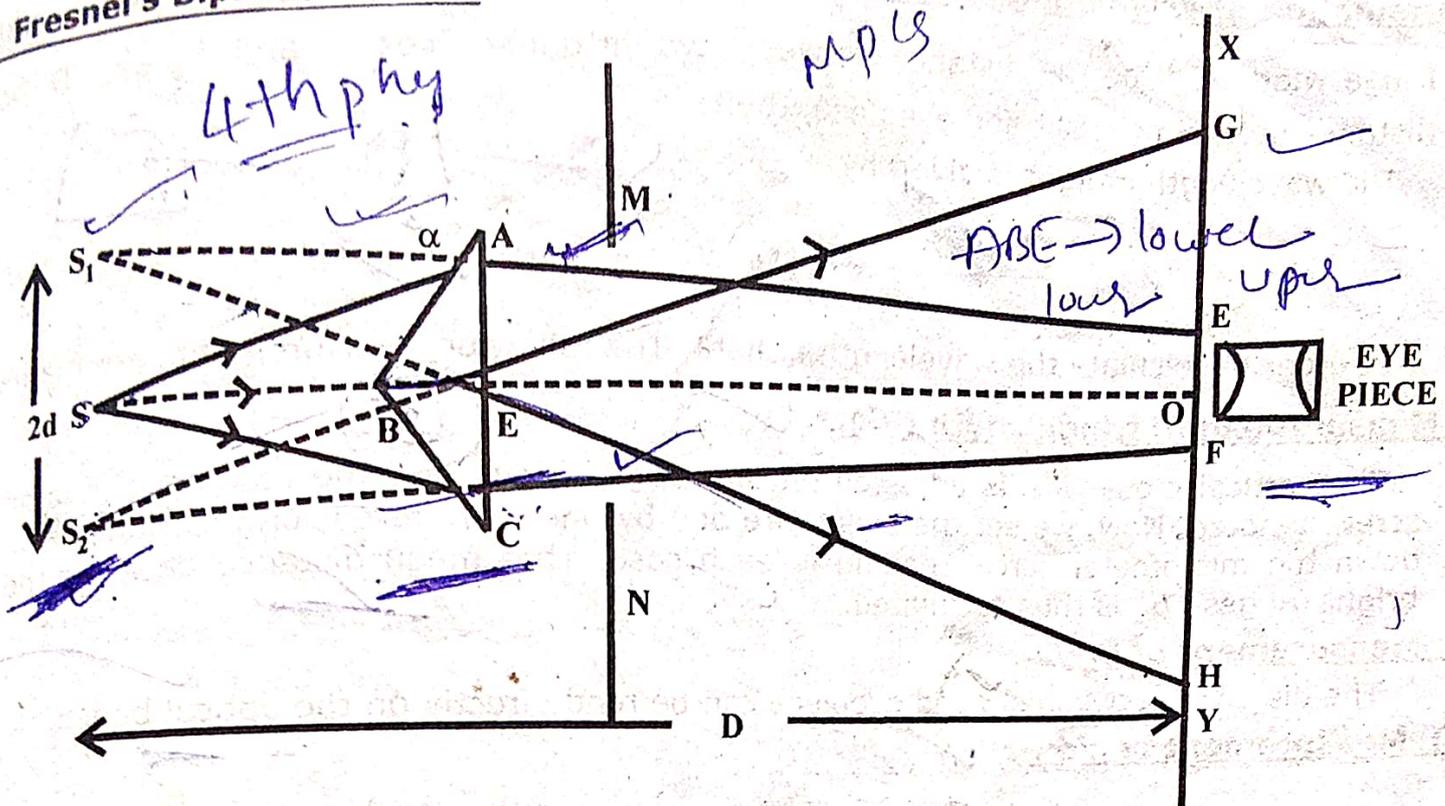
→ 1st part passes through upper half  $ABE$  of prism is deviated through small angle towards lower half of diagram & appears to diverge from  $S_1$ .

→ 2nd part passes through lower half  $CAE$  deviated through lower half towards upper half & appears to diverge from  $S_2$ .

→ Hence  $S_1$  and  $S_2$  serve as coherent sources resulting in

2 wave fronts intersect and give interference pattern which is observed by eye piece.

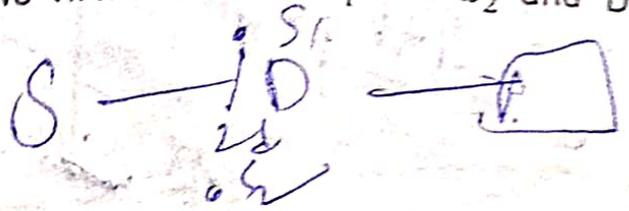
B) Fresnel's Biprism:- (IMP)



**Determination of wavelength of light:-** If ' $\lambda$ ' be the wavelength of light used, ' $\beta$ ' be the fringe width, ' $2d$ ' be the distance between two virtual sources  $S_1$  and  $S_2$  and ' $D$ ' be the distance between the slit and eyepiece, then

The wavelength of light is given by

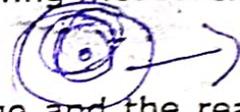
$$\lambda = \frac{\beta \cdot 2d}{D} \quad (1)$$



In order to calculate the wavelength of light, the following measurements are made.

**(i) Measurement of fringe width ( $\beta$ ):-**

The vertical cross wire is adjusted on any bright fringe and the reading of micrometer screw is noted. Now, we set the cross wire one by one on different bright fringes and note down the micrometer screw reading in each case. That mean distance between the two bright fringes ' $\beta$ ' is thus calculated.



**(ii) Measurement of  $D$ :-**

The distance between slit and eyepiece can be read directly on the optical bench.

**(iii) Measurement of ' $2d$ ':-**

For this purpose, a lens with focal length less than  $\frac{1}{4}$  of the distance between biprism and eyepiece is mounted between biprism and eyepiece as shown in fig (ii). The lens is adjusted at a position ' $L_1$ ' till sharp images of  $S_1$  and  $S_2$  are obtained in eyepiece in this case, the distance between slit and lens is objective distance ( $u$ ) while the distance between lens and eyepiece is image distance ( $v$ ). then, the magnification is given by

$$M_1 = \frac{v}{u} = \frac{d_1}{2d} \quad (1)$$

further, at the position ( $L_2$ ) of lens, the sharp images of  $S_1$  and  $S_2$  are obtained in eyepiece. Then, the distance between lens and eyepiece is objective distance ( $u$ ) while the distance between slit and lens is image distance ( $v$ ). then the magnification is given by

$$M_2 = \frac{u}{v} = \frac{d_2}{2d} \quad (2)$$

on multiplying eq'ns (1) and (2), then

$$\frac{v}{u} \times \frac{u}{v} = \frac{d_1}{2d} \times \frac{d_2}{2d}$$

$$1 = \frac{d_1 d_2}{(2d)^2}$$

$$2d = \sqrt{d_1 d_2} \quad (3)$$

$S_1 S_2$

$v = d_1 d_2$   
 $(2d) = \sqrt{d_1 d_2}$

Thus, wavelength  $\lambda$  can be determined by measuring the values  $\beta$ ,  $D$  and  $2d$ .

## Lloyd's mirror Explanation:-

Apparatus :-

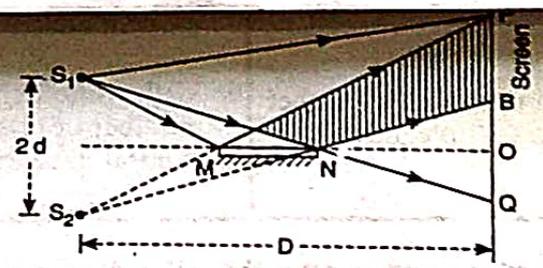
plane mirror  $MN$  and the screen.  
A narrow slit  $S_1$  is illuminated by monochromatic source of light.

Further light from slit  $S_1$  is allowed to incident on mirror  $MN$  at grazing angle.

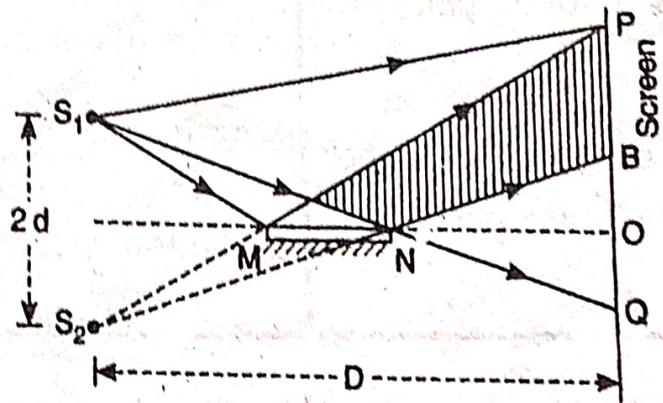
→ The reflected beam appears to diverge from  $S_2$  which is virtual image of  $S_1$ .

∴ hence  $S_1$  and  $S_2$  act as 2 coherent sources. here:

→ The direct cone of light  $PS_1A$  and reflected cone of light  $PS_2B$  super imposed over each other and produces interference fringes in overlapping region  $PS$  of screen.



Lloyd's mirror experiment: (VIMP)



## Central Fringe (Zero order fringe)

In the case of biprism we saw it has central fringe or zero order fringe is bright but here in Lloyd's mirror experiment central fringe or zero order fringe is dark.

Why because the reflected light has suffered a phase change of  $\pi$ .

So as a result of which the condition  $(2n\mu t)$  for maxima in biprism is converted into condition for minima in Lloyd's mirror.

So hence the central fringe is dark in Lloyd's mirror.

## Determination of Wavelength:-

To find wavelength, Lloyd's mirror is mounted vertically on an upright of an optical bench and placed along

upright = ...

the length of bench.

→ on another upright a narrow vertical slit is mounted which is illuminated by a monochromatic source of light.

→ At last the mirror is rotated about an axis parallel to the length of bench until fringes are observed in micrometer eye piece.

If  $\lambda$  be the wavelength of light used,  $\beta$  the fringe width,  $2d$  be the distance between  $S_1$  and  $S_2$  and  $D$  be the distance betw slit & eye piece,

⇒ wavelength of light can be found by the following formula.

$$\lambda = \frac{\beta \times 2d}{D}$$

88 points Separate Questioner  
 or Lloyd's mirror

Difference between Birefringence  
 and Lloyd's mirror fringes.

Bi prism fringes	Lloyd's mirror fringes
The central fringe is bright	The central fringe is dark.
The complete pattern of interference fringes is obtained	A few fringes are invisible here.
The fringe width is same for all pairs of coherent sources.	Fringe width is different for different pairs of coherent sources.
Condition for max intensity is, $\phi = \pm 2n\pi, n=0,1,2,\dots$	$\phi = (2n+1)\pi, n=0,1,2,\dots$
Minimum intensity condition is $\phi = (2n+1)\pi, n=0,1,2,\dots$	$\phi = \pm 2n\pi, n=0,1,2,\dots$

with produces

white light birefringence limited coloured fringes with central white

with white light Lloyd's mirror produces number of black & white fringes

Interference by 2 non-parallel reflecting surfaces.

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or

① What is wedge-shaped film. describe fringes observed when a wedge shaped film is illuminated by monochromatic light.

Wedge shaped film:-

Consider 2 plane surfaces AB and CD inclined at an angle  $\theta$  and enclosing a non-uniform thickness air film (wedge shaped film). The thickness of air film is increasing from C to D.

→ Let  $\mu$  be refractive index of film material.

→ when we pass monochromatic source of light, i.e. na. light through wedge shaped film material, the interference pattern is observed.

→ Consider a light wave PQ incident on surface AB of wedge film at an angle of incidence  $(i)$

→ As a result the rays are partly reflected as QR, & rest is refracted as QR.

later the refracted light wave  
QR again reflected from lower  
surface CD as RT, and refracted  
from surface AB, as TR<sub>2</sub>.

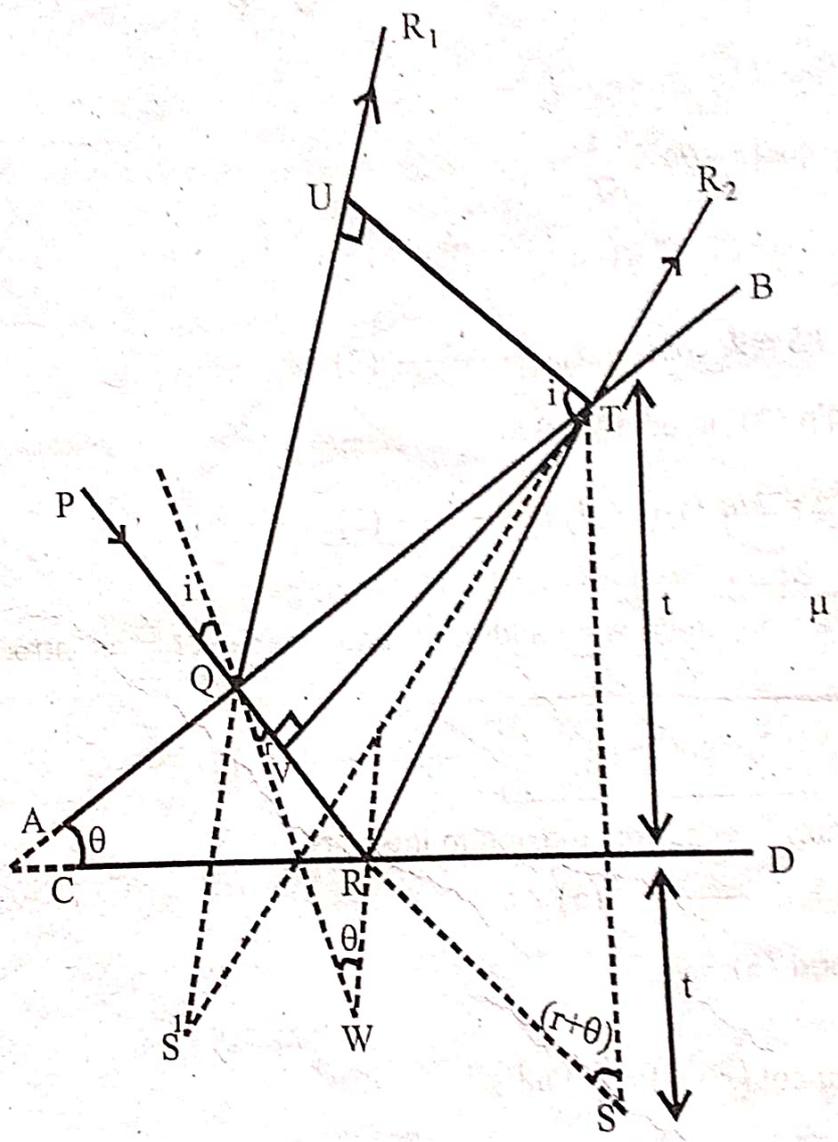
→ The waves QR<sub>1</sub> & TR<sub>2</sub> give the  
interference pattern.

→ To calculate optical path difference  
between waves QR<sub>2</sub> and QR<sub>1</sub> we  
draw 2 normals TV & TV' on QR<sub>1</sub>  
and QR<sub>2</sub> respectively.

→ later we can extend QR as  
QS as show in fig.

The optical path difference bw  
waves QR<sub>2</sub> and QR<sub>1</sub> i.e interfering  
waves is given by,

18. Interference by a film with two non-parallel reflecting surfaces (or) (WEDGE FILM):- (VVIMP)



∴ The optical path difference between (waves  $QR$  &  $RT$ ) & (waves  $QU$ ) is given by

$$\begin{aligned} \Delta &= \mu(QR + RT) - QU \\ &= \mu(QV + VR + RT) - QU \\ &= \mu(QV) + \mu(VS) - QU \quad [\because RT = RS \text{ \& } VR + RS = VS] \\ \Delta &= \mu(VS) \text{-----} (1) \quad [\because QU = \mu(QV)] \end{aligned}$$

from  $\Delta^{\text{le}}$ ,  $TVS \Rightarrow$

$$\cos(r + \theta) = \frac{VS}{ST}$$

$$VS = ST \cos(r + \theta)$$

$$VS = 2t \cos(r + \theta) \text{-----} (2)$$

sub" eq'n (2), in eq'n (1)  $\Rightarrow$

$$\Delta = 2\mu t \cos(r + \theta) \text{-----} (3)$$

but, due to reflection, there is an additional path change of  $\frac{\lambda}{2}$  is introduced. then

$$\Delta = 2\mu t \cos(r + \theta) \pm \frac{\lambda}{2} \text{-----} (4)$$

◆ For constructive interference (or) maximum intensity,

$$\Delta = n\lambda \text{-----} (5)$$

From eq'ns (4) and (5)  $\Rightarrow$

$$2\mu t \cos(r + \theta) \pm \frac{\lambda}{2} = n\lambda$$

$$\Rightarrow 2\mu t \cos(r + \theta) = (2n \pm 1) \frac{\lambda}{2} \text{-----} (6)$$

◆ For destructive Interference (or) Minimum Intensity

$$\Delta = (2n \pm 1) \frac{\lambda}{2} \quad (7)$$

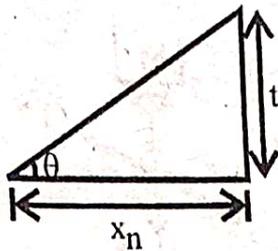
from eq'ns (4) and (7)  $\Rightarrow$

$$2\mu t \cos(r + \theta) \pm \frac{\lambda}{2} = (2n \pm 1) \frac{\lambda}{2}$$

$$\Rightarrow \boxed{2\mu t \cos(r + \theta) = \pm n\lambda} \quad (8)$$

◆ In the case of wedge shaped film,  $t$  remains constant only in direction parallel to the thin edge of wedge, hence the straight fringes parallel to the edge of the wedge are obtained.

**Fringe width (Spacing between two consecutive bright fringes):-**



For  $n^{\text{th}}$  maxima,

$$2\mu t \cos(r + \theta) = (2n + 1) \frac{\lambda}{2} \quad (9)$$

for normal incidence and air film,

$$r = 0 \text{ \& } \mu = 1$$

from eq'n (9)  $\Rightarrow$

$$2t \cos \theta = (2n + 1) \frac{\lambda}{2} \quad (10)$$

from, the fig.

$$\text{Tan} \theta = \frac{t}{x_n}$$

$$\Rightarrow t = x_n \text{ Tan} \theta \quad (11)$$

Sub" eq'n (11), in equation (10)  $\Rightarrow$

$$2x_n \text{ Tan} \theta \cdot \cos \theta = (2n + 1) \frac{\lambda}{2}$$

$$2x_n \sin \theta = (2n + 1) \frac{\lambda}{2} \quad (12)$$

If the  $(n+1)^{\text{th}}$  maximum is obtained at a distance  $x_{n+1}$  from thin edge, then

$$2x_{n+1} \sin \theta = [2(n+1) + 1] \frac{\lambda}{2}$$

$$\Delta = (2n \pm 1) \frac{\lambda}{2} \quad (7)$$

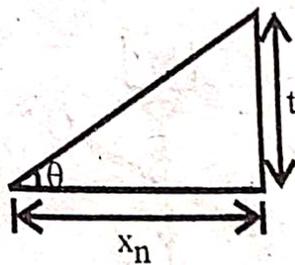
from eq'ns (4) and (7)  $\Rightarrow$

$$2\mu t \cos(r + \theta) \pm \frac{\lambda}{2} = (2n \pm 1) \frac{\lambda}{2}$$

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If the  $(n+1)^{\text{th}}$  maximum is obtained at a distance  $x_{n+1}$  from thin edge, then

$$2x_{n+1} \sin \theta = [2(n+1) + 1] \frac{\lambda}{2}$$

$$2x_{n+1} \sin \theta = (2n+3) \frac{\lambda}{2} \quad (13)$$

on subtracting eq'n (12) from eq'n (13)  $\Rightarrow$

$$2x_{n+1} \sin \theta - 2x_n \sin \theta = (2n+3) \frac{\lambda}{2} - (2n+1) \frac{\lambda}{2}$$

$$2(x_{n+1} - x_n) \sin \theta = (2n+3 - 2n-1) \frac{\lambda}{2}$$

$$2\beta \sin \theta = \lambda$$

$$\Rightarrow \beta = \frac{\lambda}{2 \sin \theta}$$

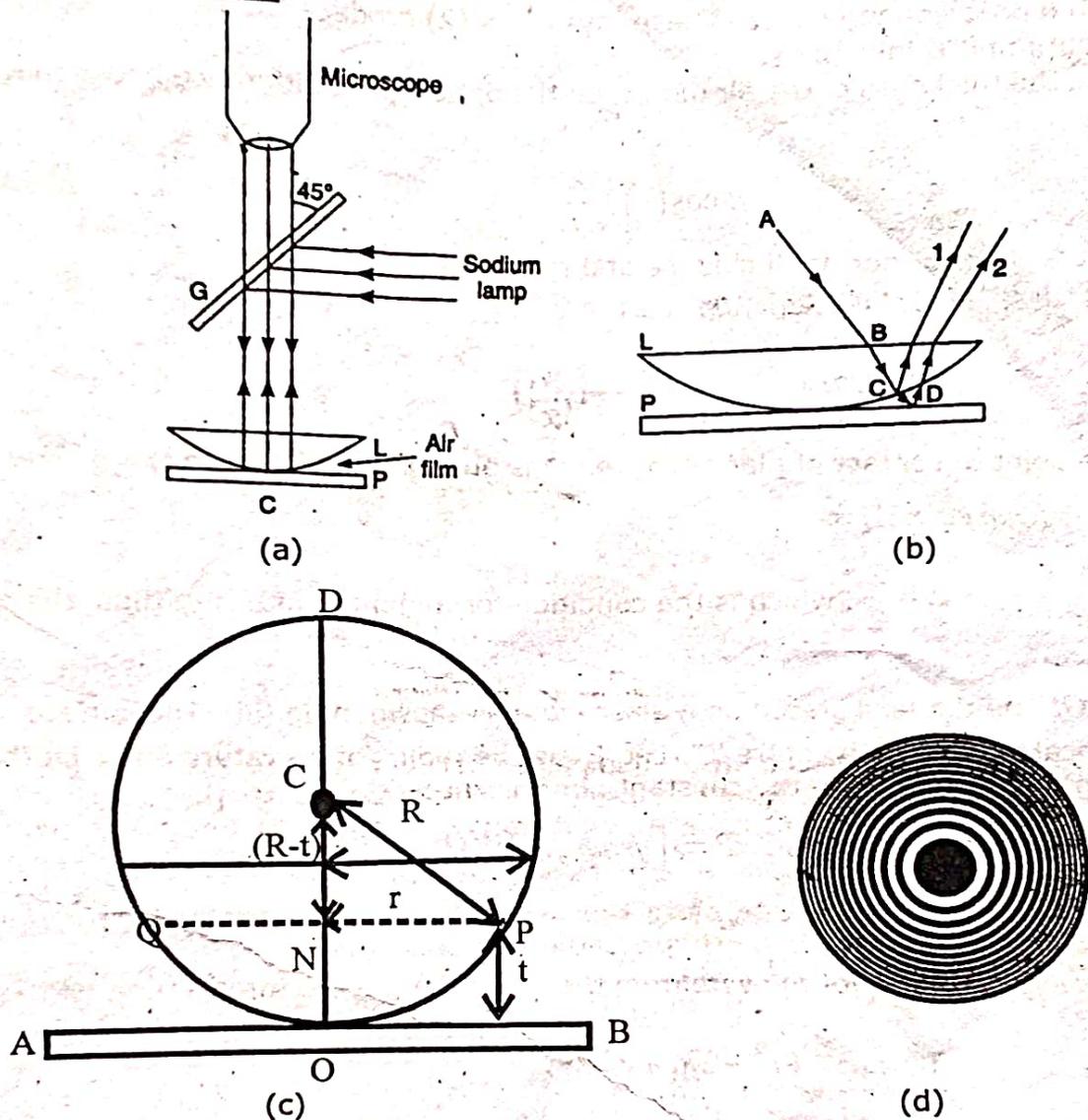
$$[\because x_{n+1} - x_n = \beta]$$

$$\boxed{\beta = \frac{\lambda}{2\theta}} \quad (14) \quad [\because \theta \text{ is very small} \Rightarrow \sin \theta = \theta]$$

### 19) Newton's Rings: (Reflected light):- (VVIMP)

When a plano-convex lens with its convex surface is placed on a plane glass plate, an air film of gradually increasing thickness is formed between convex lens and plane glass plate. The thickness of the film at the point of contact is zero. If monochromatic light is allowed to fall normally, and the film is viewed in reflected light, alternate dark and bright rings concentric around the point of contact between the lens and glass plate are observed are known as Newton's rings.

#### Experimental arrangement:-



The Newton's rings experimental arrangement is shown in fig. It consists of mainly three parts namely sodium vapour lamp with a plane glass plate (G) at an angle  $45^\circ$  with the vertical travelling MICROSCOPE (M) and the combination of plano-convex lens 'L' and plane glass plate (P).

A parallel beam of monochromatic light from an extended source is made incident on a inclined glass plate (G), which reflects it in vertically downward direction. Each ray of light suffers reflections from upper and lower surfaces of thin air film formed between plano-convex lens and plane glass plate. These reflected rays of light superimpose and produce an interference pattern consisting of alternate dark and bright rings as shown in fig.

- ◆ As locus of all the points of air film of same thickness, is a circle. So Interference fringes due to all the rays of incident light at points corresponding to a particular thickness of air film, merge to appear as a circular ring.

- ◆ Central ring is dark and the thickness of rings goes on decreasing as we move away from central ring. because the thickness of air film goes on increasing as we move away from point of contact of plano-convex lens with plane glass plate.
- ◆ Newton's rings are Localised fringes.

**Theory:**

AB is a monochromatic ray of light which falls on the system as shown in fig (ii). A part reflected at C which goes out in the form of ray (1) without any phase change. The rest part is refracted along CD. at point 'D' it is again reflected and goes out in the form of ray (2) with a phase change of  $\pi$ . These rays (1) & (2) produce Interference pattern consisting of alternate dark and Bright rings.

If 't' be the thickness of the air film, then the optical path difference between rays (1) & (2) is given by

$$\Delta = 2\mu t \cos(r) + \frac{\lambda}{2}$$

for normal incidence and an air film

$$r = 0 \text{ and } \mu = 1$$

$$\therefore \Delta = 2t + \frac{\lambda}{2} \text{ ————— (1)}$$

at the point of contact of plano-convex lens and plane glass plate,  $t = 0$ , then

from eq'n (1)  $\Rightarrow$

$$\Delta = \frac{\lambda}{2}, \text{ which is the condition for minimum intensity thus, the central spot}$$

is dark.

Let  $LOL^1$  be the lens placed on a glass plate as shown in fig (iii). The surface  $LOL^1$  is the part of spherical surface with centre 'C'. Let 'R' be the radius of curvature and r be the radius of Newton's ring corresponding to the constant film thickness 't'.

from  $\Delta^{le}$  Triangle,  $CNP \Rightarrow$  [from fig (iii)]

$$CP^2 = CN^2 + NP^2$$

$$R^2 = (R-t)^2 + r^2$$

$$R^2 = R^2 + t^2 - 2Rt + r^2$$

$$\Rightarrow r^2 = 2Rt - t^2 = 2Rt \quad \left[ \because t \ll R \Rightarrow t^2 \text{ can be Neglected comparable to } 2Rt \right]$$

$$\Rightarrow t = \frac{r^2}{2R} \text{ ————— (2)}$$

sub" eq'n (2), in eq'n (1)  $\Rightarrow$

$$\Delta = \frac{2r^2}{2R} + \frac{\lambda}{2}$$

$$\Rightarrow \Delta = \frac{r^2}{R} + \frac{\lambda}{2} \text{ ————— (3)}$$

### Diameter of Bright ring:-

for the Bright ring / maximum Intensity

$$\Delta = n\lambda \text{ ————— (4)}$$

from eq'ns (3) & (4)  $\Rightarrow$

$$\frac{r^2}{R} + \frac{\lambda}{2} = n\lambda$$

$$\frac{r^2}{R} = n\lambda - \frac{\lambda}{2}$$

$$\frac{r^2}{R} = (2n-1)\frac{\lambda}{2}$$

$$r^2 = \frac{(2n-1)\lambda R}{2}$$

$$\left(\frac{D_b}{2}\right)^2 = \frac{(2n-1)\lambda R}{2} \quad [ \because D_b = 2r ]$$

$$\frac{D_b^2}{4} = \frac{(2n-1)\lambda R}{2}$$

$$D_b^2 = 2(2n-1)\lambda R$$

$$D_b = \sqrt{2(2n-1)\lambda R}$$

$$\boxed{D_b \propto \sqrt{(2n-1)}} \text{ ————— (5)}$$

Thus, the diameters of the bright rings are proportional to the square roots of odd natural numbers.

### Diameter of dark ring:-

For the dark ring / Minimum Intensity

$$\Delta = (2n+1)\frac{\lambda}{2} \text{ ————— (6)}$$

from eq'ns (3) & (6)  $\Rightarrow$

$$\frac{r^2}{R} + \frac{\lambda}{2} = (2n+1)\frac{\lambda}{2}$$

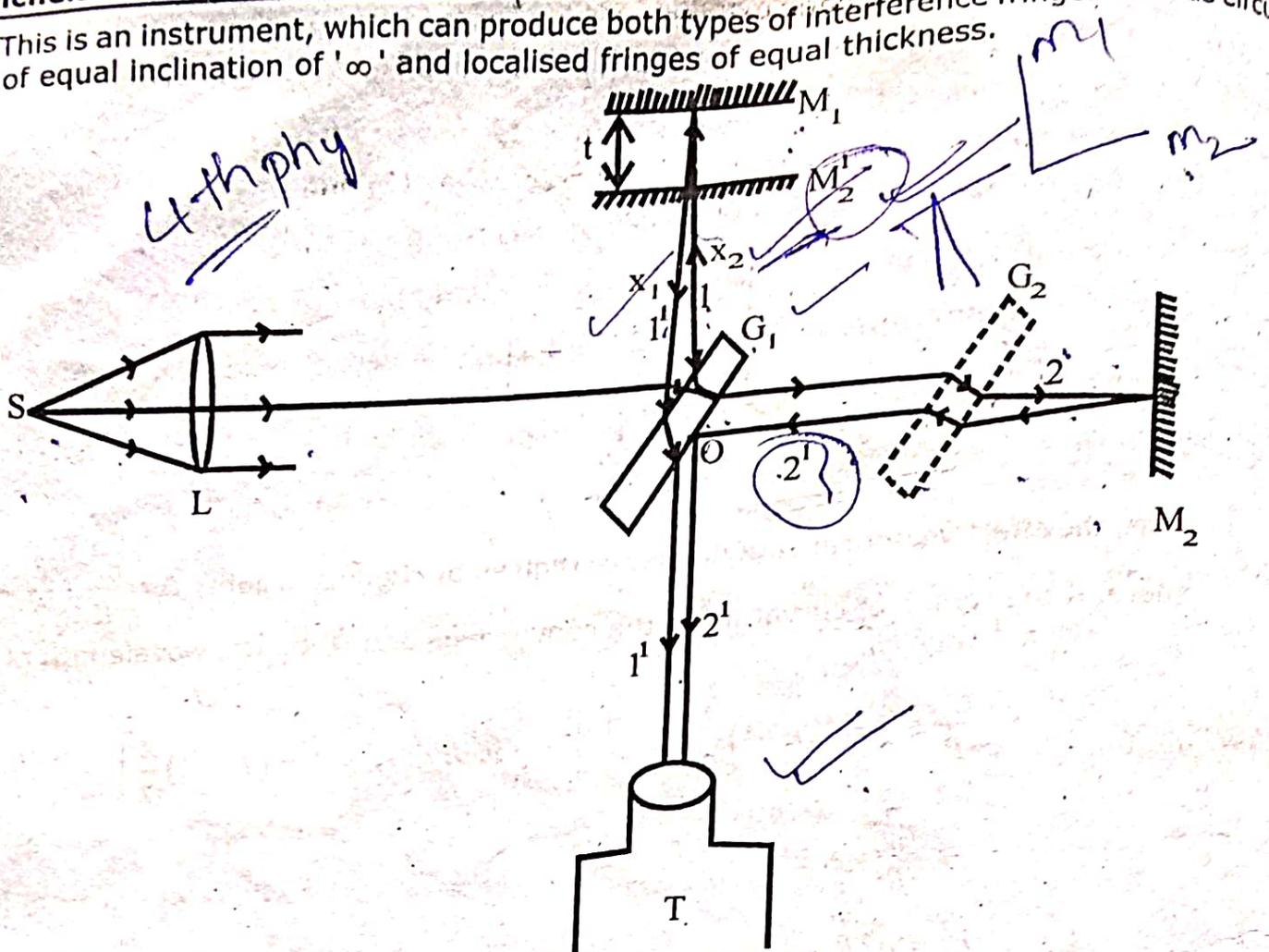
$$\frac{r^2}{R} + \frac{\lambda}{2} = n\lambda + \frac{\lambda}{2}$$

$$\frac{r^2}{R} = n\lambda$$

$$r^2 = n\lambda R$$

**23) Michelson's Interferometer:- (ht IMP)**

This is an instrument, which can produce both types of interference fringes such as circular fringes of equal inclination of ' $\infty$ ' and localised fringes of equal thickness.



- $M_1$  &  $M_2 \rightarrow$  Plane mirrors ✓
- $G_1$  &  $G_2 \rightarrow$  Plane Glass plates ✓
- $T \rightarrow$  Telescope ✓
- $S \rightarrow$  Monochromatic extended source ✓
- $L \rightarrow$  Convex lens ✓
- $M_2' \rightarrow$  Virtual Image of  $M_2$  ✓

**Construction:-**

The Michelson's interferometer is shown in fig. It consists of two plane mirrors  $M_1$  and  $M_2$  which are at right angles to each other.  $M_1$  can be moved such that its new position is parallel to its previous position while  $M_2$  is fixed.  $M_1$  and  $M_2$  are provided with three levelling screws at their backs. With the help of these screws the mirror can be tilted about horizontal and vertical axes so that they can be made exactly perpendicular to each other. There are two plane glass plates  $G_1$  and  $G_2$  of same thickness and of the same material placed parallel to each other.

These plates are also inclined at an angle  $45^\circ$  with the mirror  $M_1$  and  $M_2$ .

The face of  $G_1$  towards  $G_2$  is semi-silvered.  $T$  is a Telescope which receives the reflected lights from  $M_1$  and  $M_2$ .



**Working:-**

Light from a monochromatic extended source 'S' after being rendered by a collimating lens 'L' falls on the semisilvered glass plate  $G_1$ . at  $G_1$  incident light splits into two parts. One being reflected as ray (1) and which travels towards Mirror  $M_1$  and again reflected as ray '1<sup>1</sup>' and again reaches the glass plate  $G$ ; the second being refracted as ray (2) and which travels towards Mirror  $M_2$  and again reflected as ray 2<sup>1</sup> and again reaches the glass plate  $G_1$ . ray 2 and 2<sup>1</sup> passes through compensating plate  $G_2$ . Thus, the paths Travelled by two rays (1&2) are equal. These two rays 1<sup>1</sup> & 2<sup>1</sup> gives the Interference pattern. It can be observed in the Telescope 'T'.

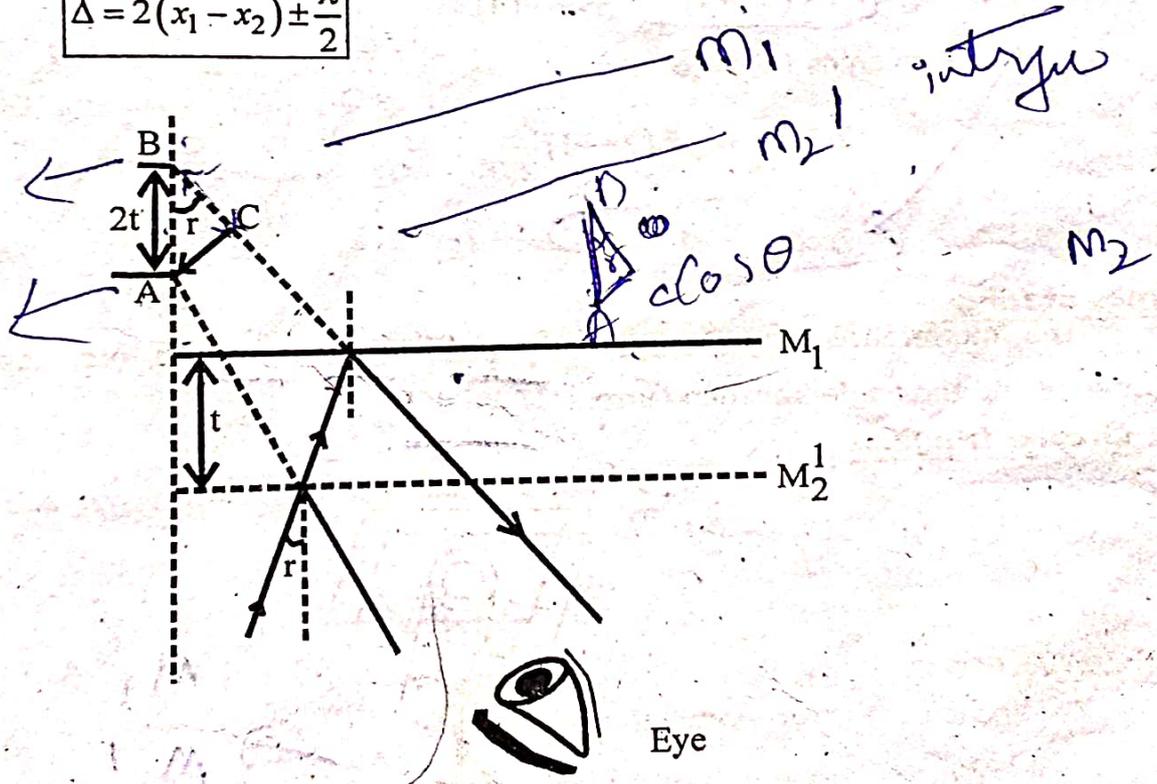
If we see in the direction of  $M_1$ , one observes  $M_1$  and also a virtual Image  $M_2^1$  of  $M_2$ . Thus, the two interfering beams come by reflection from Mirror  $M_1$  and  $M_2^1$ .

If the distance  $OM_1 = x_1$  and  $OM_2^1 = x_2$ , then

The path difference between interfering rays (waves) is given by

$$\Delta = 2(x_1 - x_2) \pm \frac{\lambda}{2}$$

**Theory:-**



When you are observing interference pattern, in the direction of  $M_1$ , the two interfering beams come from points A and B as shown in fig. hence the optical path difference between two beams is 'BC'.

from  $\Delta^{le} BAC \Rightarrow$

$$\cos r = \frac{BC}{AB}$$

$$\Rightarrow BC = AB \cos r$$

$$BC = 2t \cos r \text{ and}$$

but, due to reflection, there is an additional path difference of  $\frac{\lambda}{2}$  is introduced. Then the effective path difference is given by

$$\Delta = 2t \cos r + \frac{\lambda}{2} \quad (1)$$

for maximum intensity,

$$\Delta = n\lambda \quad (2)$$

from eq'ns (1) & (2)  $\Rightarrow$

$$2t \cos r + \frac{\lambda}{2} = n\lambda$$

$$2t \cos r = (2n-1) \frac{\lambda}{2} \quad (3)$$

for minimum intensity

$$\Delta = (2n+1) \frac{\lambda}{2} \quad (4)$$

from eq'ns (1) & (4)  $\Rightarrow$

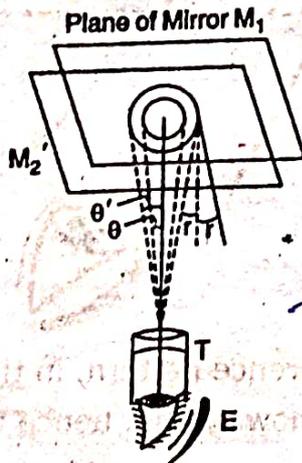
$$2t \cos r + \frac{\lambda}{2} = (2n+1) \frac{\lambda}{2}$$

$$2t \cos r = n\lambda \quad (5)$$

### Types of fringes:-

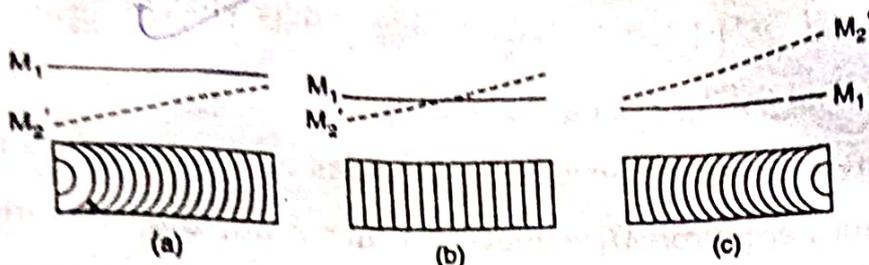
The interference fringes may be straight, circular, parabolic, etc. depending upon path difference and the angle between Mirrors  $M_1$  and  $M_2$ .

#### 1) Circular fringes:-



When mirror  $M_2$  is exactly perpendicular to mirror  $M_1$  (or) Mirror  $M_1$  and  $M_2$  are parallel an air film of constant thickness is enclosed between them. It can be seen from fig. that the path differences are different for different values of ' $\theta$ '. Hence, the path rings while the path difference which satisfies the condition of maxima appears bright rings while the path difference which satisfies the condition of minima appears dark rings. These are formed at infinity hence they are observed through a Telescope focused at infinity.

## 2) Localised fringes:-



When the mirror  $M_2$  is not exactly perpendicular to mirror  $M_1$  (or) the mirror  $M_1$  and the virtual image  $M_2'$  are inclined, the air film, enclosed between them is wedge-shaped. The shape of fringes depends on the thickness of the film and the angle of incidence.

When the two mirrors  $M_1$  and  $M_2'$  intersect in the middle, straight fringes are observed. When the two mirrors are inclined, curved fringes with convexity towards the thin edge of the wedge are observed as shown in fig.

## 3) Localised white light fringes:-

When monochromatic light source is replaced by a white source, then coloured and curved localised fringes are obtained. The fringes of zero thickness being again perfectly dark and straight. Other fringes are coloured due to overlapping of various colours. If the film is thick, uniform illumination is observed.

## 24) Uses of Michelson's Interferometer:-

### i) Determination of wavelength of monochromatic source of Light:-

Initially the Michelson interferometer is set for circular fringes with central bright spot. If 't' be the thickness of the air film between two mirrors and 'n' be the order of the spot obtained,

then for the normal incidence ( $r=0$ ),  $2t + \frac{\lambda}{2} = n\lambda$  ————— (1) *Types use*

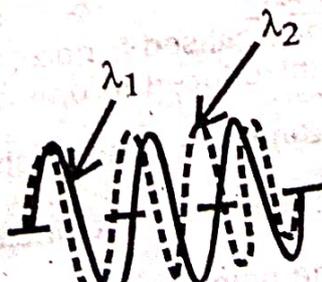
If, now  $M_1$  is moved  $\frac{\lambda}{2}$  away from  $M_2'$ , then  $(n+1)^{th}$  bright spot appears at the centre of the field. Let N be the number of fringes that cross the centre of field when the mirror  $M_1$  is moved from initial position  $x_1$  to a final position  $x_2$ , then

$$N \frac{\lambda}{2} = x_2 - x_1$$

$$\Rightarrow N\lambda = 2(x_2 - x_1)$$

$$\lambda = \frac{2(x_2 - x_1)}{N}$$

### ii) Determination of difference in wavelength of sodium $D_1, D_2$ lines (or) Determination of difference in wavelengths of spectral lines :- (V IMP)



$$n \rightarrow 3 \rightarrow \lambda_1$$

$$(n+1) \rightarrow 4 \rightarrow \lambda_2$$

$(\lambda_1 > \lambda_2)$

Initially Michelson Interferometer is set for circular fringes. Let the source have wavelengths say  $\lambda_1$  and  $\lambda_2$  ( $\lambda_1 > \lambda_2$ ) which are very close to each other. The two wavelengths form their separate fringe patterns but as  $\lambda_1$  and  $\lambda_2$  are very close to each other and thickness of air film is small, the two patterns practically coincide. As the mirror  $M_1$  is moved slowly, the patterns separated, further mirror  $M_1$  is moved in such a way that maximum intensity (bright) corresponds to  $\lambda_1$  coincides with the maximum intensity (bright) corresponds to  $\lambda_2$ . The position of mirror  $M_1$  is noted as  $x_1$ . Further mirror  $M_1$  is moved in such a way that  $n^{\text{th}}$  bright of  $\lambda_1$  coincides with  $(n+1)^{\text{th}}$  bright of  $\lambda_2$ .

Now, the position of mirror  $M_1$  is noted as  $x_2$ . Let  $x[x_2 - x_1]$  be the effective distance between mirrors  $M_1$  &  $M_2$ . Then

$$2x = n\lambda_1 \quad \text{--- (1) \&}$$

$$2x = (n+1)\lambda_2 \quad \text{--- (2)}$$

from eq'n (1)  $\Rightarrow$

$$n = \frac{2x}{\lambda_1} \quad \text{--- (3)}$$

from eq'n (2)  $\Rightarrow$

$$(n+1) = \frac{2x}{\lambda_2} \quad \text{--- (4)}$$

(4) - (3)  $\Rightarrow$

$$(n+1) - n = \frac{2x}{\lambda_2} - \frac{2x}{\lambda_1}$$

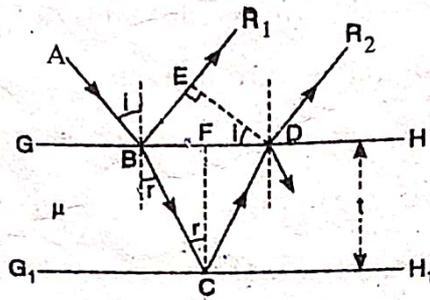
$$1 = \frac{2x\lambda_1 - 2x\lambda_2}{\lambda_1\lambda_2}$$

$$\Rightarrow 2x(\lambda_1 - \lambda_2) = \lambda_1\lambda_2$$

$$\boxed{\lambda_1 - \lambda_2 = \frac{\lambda_1\lambda_2}{2x} = \frac{\lambda_{\text{avg}}^2}{2x}}$$

$$\left[ \because \lambda_{\text{avg}} = \frac{\lambda_1 + \lambda_2}{2} \right]$$

**13). Oblique incidence of a plane wave on a thin film due to reflected light:- (Cosine Law)**



Let  $GH$  and  $G_1H_1$  be the two surfaces of Transparent film of uniform thickness ' $t$ ' and Refractive index ' $\mu$ ' as shown in fig. Suppose a ray  $AB$  of monochromatic light is incident on its upper surface. This ray is partly reflected along  $BR_1$  and refracted along  $BC$ . After one reflection at ' $C$ ', we obtain the ray  $CD$ . After refraction at  $D$ , the ray finally emerges out along  $DR_2$  in air. Obviously  $DR_2$  is parallel to  $BR_1$  in order to calculate the path difference between the rays, we draw a normal  $DE$  on  $BR_1$ .

The path difference between the rays is given by

$$\Delta = \mu(BC + CD) - BE \quad (1)$$

From the  $\Delta^{le} BCF \Rightarrow$

$$\cos r = \frac{CF}{BC}$$

$$\cos r = \frac{t}{BC}$$

$$\Rightarrow BC = CD = \frac{t}{\cos r} \quad (2)$$

from the  $\Delta^{le} BCF \Rightarrow$

$$\tan r = \frac{BF}{FC}$$

$$\Rightarrow BF = FC \tan r$$

$$BF = t \tan r \quad \&$$

$$BD = BF + FD$$

$$BD = 2BF = 2t \tan r$$

from the  $\Delta^{le} BED \Rightarrow$

$$\sin i = \frac{BE}{BD}$$

$$\Rightarrow BE = BD \sin i$$

$$BE = 2t \tan r \sin i \quad (3)$$

we know that,

$$\mu = \frac{\sin i}{\sin r}$$

$$\Rightarrow \sin i = \mu \sin r \quad (4)$$

sub|| eq'n (4) in eq'n (3)  $\Rightarrow$

$$BE = 2t \tan r (\mu \sin r)$$

$$BE = 2\mu t \tan r \sin r \quad (5)$$

sub|| eq'ns (2) & (5), in eq'n (1)  $\Rightarrow$

$$\Delta = \mu \left( \frac{t}{\cos r} + \frac{t}{\cos r} \right) - 2\mu t \tan r \sin r$$

$$\Delta = \frac{2\mu t}{\cos r} [1 - \sin^2 r]$$

$$\Delta = \frac{2\mu t}{\cos r} \cos^2 r$$

$$\boxed{\Delta = 2\mu t \cos r} \text{ ————— (6)}$$

This is known as cosine law.

**14) Oblique incidence of a plane wave on a thin film due to transmitted light (cosine law):-**

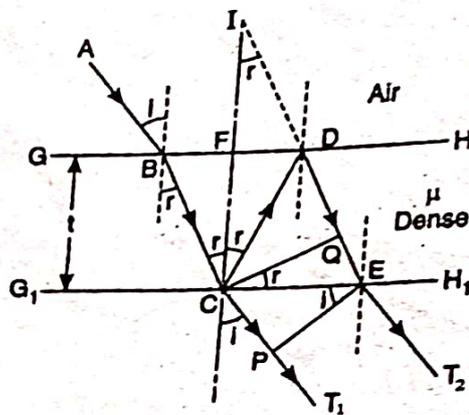


Fig. shows the geometry of the transmitted light to produce interference pattern. Due to simultaneous reflection and refraction we obtain two transmitted rays  $CT_1$  and  $ET_2$ . These two rays have a constant phase difference. In order to calculate the path difference between the two transmitted rays, we draw normal  $CQ$  on  $DE$  and  $EP$  on  $CT_1$  and we also produce  $ED$  in the backward direction which meets produced  $CF$  at  $I$ .

The path difference between two transmitted rays is given by

$$\Delta = \mu(CD + DE) - CP \text{ ————— (1)}$$

from  $\Delta^{le} CPE \Rightarrow$

$$\sin i = \frac{CP}{CE} \text{ \&}$$

from  $\Delta^{le} CQE \Rightarrow$

$$\sin r = \frac{QE}{CE}$$

We know that

$$\therefore \mu = \frac{\sin i}{\sin r}$$

$$\mu = \frac{\frac{CP}{CE}}{\frac{QE}{CE}} = \frac{CP}{QE}$$

$$\Rightarrow CP = \mu(QE) \text{ ————— (2)}$$

Sub" eq'(2), in eq'n (1)  $\Rightarrow$

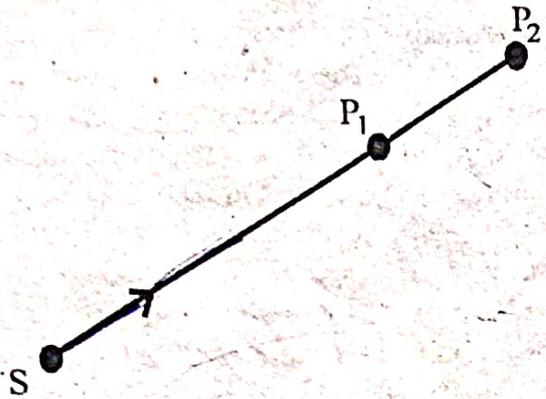
$$\begin{aligned}\Delta &= \mu(CD + DE) - \mu(QE) \\ &= \mu(CD + DQ + QE) - \mu(QE) \\ &= \mu(CD + DQ) \\ &= \mu CI\end{aligned}$$

$$\Delta = 2\mu t \cos r \text{ ————— (3)}$$

#### 4) Temporal Coherence :- (VIMP)

Temporal coherence is the measure of the average correlation between the value of a wave and it self delayed by (coherence time) " $\tau$ " at any pair of times. i.e. it characterizes how well a wave can interfere with itself at different time.

It describes the correlation between waves observed at different moments in time.



S - Source of light

$P_1, P_2$  - Two points on the same wave at different moments of time

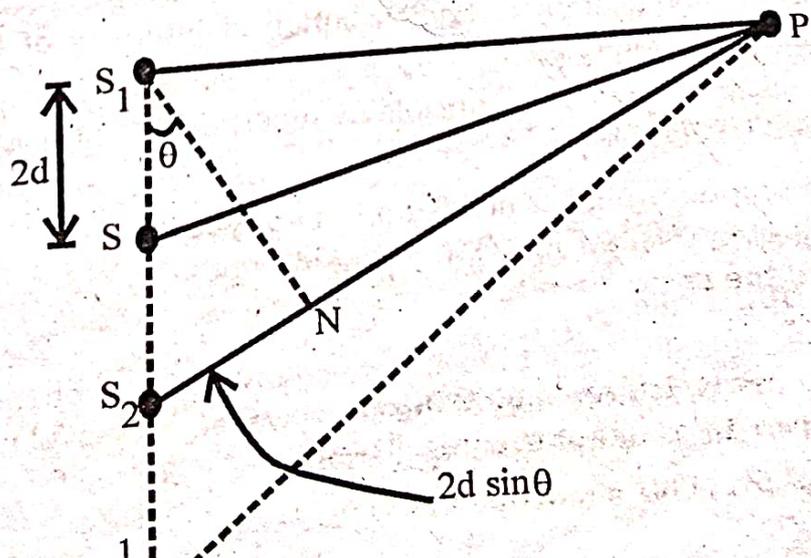
consider a monochromatic source of light 'S' and Two points  $P_1$  &  $P_2$  on the same wave as shown in fig. consider the situation in which the path of wave is extended. hence, the phase difference between  $P_1$  and  $P_2$  will depend on distance between points  $P_1$  and  $P_2$  and coherence length.

- ◆ If the distance between  $P_1$  &  $P_2$  is less than coherence length, then the wave maintains constant phase difference between  $P_1$  and  $P_2$  and takes place interference pattern.
- ◆ If the distance between  $P_1$  &  $P_2$  is greater than coherence length, then there is no phase relation as a result interference fringes lose sharpness or contrast.

#### 5) Spatial coherence :- (IMP)

If the phase difference for any two fixed points in a plane normal to the wave propagation does not vary with time, then the wave is said to exhibit spatial coherence.

- ◆ Spatial coherence describes the correlation between waves at different points in space.
- ◆ In general, it is the condition for path difference between waves to produce interference pattern.



Let  $S_1$  and  $S_2$  be two sources (atomic emitters) and P be a point of observation as shown in fig. Then the path difference between the waves is given by

$$S_2P - S_1P = 2d \sin \theta$$

in general, the emission time of an atom is  $10^{-9}$  sec. hence the corresponding length is  $C \times 10^{-9}$ .

◆ To produce interference pattern, the path difference should be less than that  $C \times 10^{-9}$ .

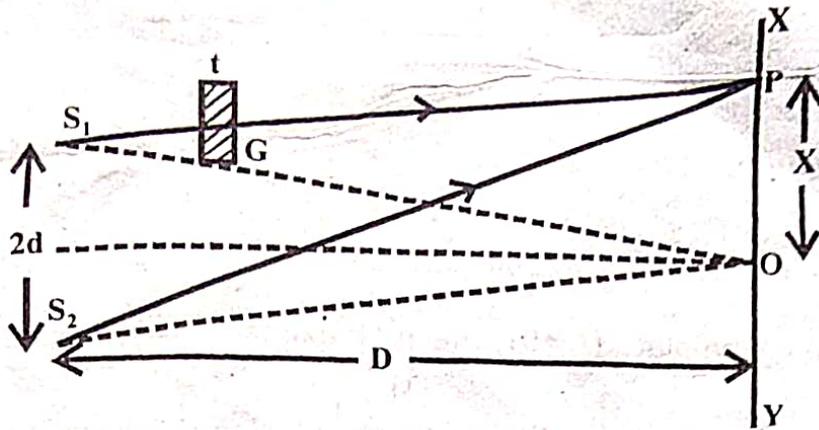
$$\therefore S_2P - S_1P = 2d \sin \theta \leq C \times 10^{-9} \left[ \begin{array}{l} \text{in our consideration} \\ \text{it is valid for } S_1 \text{ \& } S_2 \end{array} \right]$$

Now, the source  $S_2$  be drawn a part to a position  $S_2^1$ .

Then, the path difference becomes  $(S_2^1P - S_1P)$  and the spatial coherence becomes poorer.

i.e. If the path difference b/w two waves is greater than ' $C \times 10^{-9}$ ', the interference fringes lose sharpness or contrast.

9) Determination of thickness of a Transparent material using Biprism:- (VVIMP)



The Biprism experiment can be used to determine the thickness of a thin sheet of transparent material such as glass, mica etc. When a thin Transparent sheet of thickness 't' and refractive index ' $\mu$ ' is introduced in the path of one of the interfering beams as shown in fig, The entire fringe system is displaced through a constant distance towards the path of the beam in which the plate is introduced. Now, we consider the path  $S_1P$ . The length  $(S_1P - t)$  of this path is travelled in air with the velocity of light C, while the length 't' is travelled in mica with velocity  $C_g$ .

$\therefore$  The time taken by a wave to travel from  $S_1$  to  $P = \frac{(S_1P - t)}{C} + \frac{t}{C_g}$

" "  $= \frac{S_1P - t}{C} + \frac{\mu t}{C} \left[ \begin{array}{l} \because \mu = \frac{C}{C_g} \\ \Rightarrow C_g = \frac{C}{\mu} \end{array} \right]$

" "  $= \frac{S_1P - t + \mu t}{C}$

" "  $= \frac{S_1P + (\mu - 1)t}{C}$

$\therefore$  The path  $S_1$  to P is equivalent to an air path  $= S_1P + (\mu - 1)t$

$\therefore$  The path difference at P  $= S_2P - S_1P - (\mu - 1)t$

$\therefore$  The path difference at P  $= \frac{2xd}{D} - (\mu - 1)t$  ————— (1)  $\left[ \because S_2P - S_1P = \frac{2xd}{D} \right]$

But, we know that, for  $n^{th}$  maxima

The path difference at P  $= n\lambda$  ————— (2)

from eq'ns (1) & (2)  $\Rightarrow$

$$\frac{2x_n d}{D} - (\mu - 1)t = n\lambda \quad \left[ \because \text{for } n^{\text{th}} \text{ fringe } \frac{2xd}{D} = \frac{2x_n d}{D} \right]$$

$$\frac{2x_n d}{D} = n\lambda + (\mu - 1)t$$

$$\Rightarrow x_n = \frac{D}{2d} [n\lambda + (\mu - 1)t] \quad \text{--- (3)}$$

In the absence of the plate ( $t = 0$ ), the  $n^{\text{th}}$  maxima  $= \frac{Dn\lambda}{2d}$

If 'S' is the displacement of  $n^{\text{th}}$  maxima by introducing the mica, then

$$S = \frac{D}{2d} [n\lambda + (\mu - 1)t] - \frac{Dn\lambda}{2d}$$

$$\Rightarrow S = \frac{Dn\lambda}{2d} + \frac{D}{2d} (\mu - 1)t - \frac{Dn\lambda}{2d}$$

$$S = \frac{D}{2d} (\mu - 1)t$$

$$\Rightarrow t = \frac{S \times 2d}{(\mu - 1)D} \quad \text{--- (4)}$$

Speed =  $\frac{\text{dis}}{\text{time}}$

use  $\rightarrow$  ?

$S_1 \rightarrow P$

$S_2 \rightarrow M$

$\Rightarrow S_2 - P - S_1 \rightarrow P$

$\Rightarrow$  path diff

$n^{\text{th}}$  fringe  $\rightarrow$

$t = 0 \rightarrow S_2 \rightarrow M$

$S = x_n - x_0$